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Application of Dual-Polarimetry SAR Images in Multitemporal InSAR Processing

Mostafa Esmaeili, Mahdi Motagh, and Andy Hooper

Abstract—Multitemporal polarimetric synthetic aperture radar (SAR) data can be used to estimate the dominant scattering mechanism of targets in a stack of SAR data and to improve the performance of SAR interferometric methods for deformation studies. In this letter, we developed a polarimetric form of amplitude difference dispersion (ADD) criterion for time-series analysis of pixels in which interferometric noise shows negligible decorrelation in time and space in small baseline algorithm. The polarimetric form of ADD is then optimized in order to find the optimum scattering mechanism of the pixels, which in turn is used to produce new interferograms with better quality than single-pol SAR interferograms. The selected candidates are then combined with temporal coherency criterion for final phase stability analysis in full-resolution interferograms. Our experimental results derived from a data set of 17 dual polarizations X-band SAR images (HH/VV) acquired by TerraSAR-X shows that using optimum scattering mechanism in the small baseline method improves the number of pixel candidates for deformation analysis by about 2.5 times in comparison with the results obtained from single-channel SAR data. The number of final pixels increases by about 1.5 times in comparison with HH and VV in small baseline analysis. Comparison between persistent scatterer (PS) and small baseline methods shows that with regards to the number of pixels with optimum scattering mechanism, the small baseline algorithm detects 10% more pixels than PS in agricultural regions. In urban regions, however, the PS method identifies nearly 8% more coherent pixels than small baseline approach.

Index Terms—Amplitude difference dispersion (ADD), polarimetric optimization, slowly decorrelating filtered phase (SDFP), Tehran plain.

I. INTRODUCTION

INTERFEROMETRIC analysis of synthetic aperture radar (SAR) data is a powerful geodetic technique to measure surface deformations [1]–[4]. The accuracy achieved with interferometric measurements depends on a variety of factors including temporal and geometrical decorrelation, variations in atmospheric water vapor between SAR data acquisitions and the accuracy of orbital and digital elevation model used in the processing [5]. In order to address these limitations, multitemporal InSAR (MTI) time-series processing techniques such as small baseline algorithms and persistent scatterer InSAR (PSI) have been developed.

The main goal of these techniques is to identify pixels for which the effect of the interferometric noise is small, so that they remain stable over the whole period of SAR data acquisition [6]–[8].

The PSI technique, first proposed by Ferretti et al. [6], [7], presents a solution to deal with spatiotemporal decorrelations of interferometric phase using time-series analysis of single-master interferograms. The technique uses amplitude dispersion index (ADI) as a proxy of phase stability to identify pixels whose scattering properties are coherent between SAR image acquisition with long time interval and different look angles, the so-called permanent scatterer (PS). As interferograms are generated with a common master, PSs are limited to those pixels that show high coherence even in interferograms with larger baselines than the critical baseline [6], [7]. In [8], a new PS technique was proposed in which both amplitude and phase criteria are assessed to determine the stability of PSs. An initial set of candidate pixel based on amplitude analysis is selected first and then in an iterative process, the PS probability is refined using phase analysis. The method is more suitable for detecting low-amplitude PS pixels in natural terrains, where the relationship between ADI index and phase stability breaks down.

Small baseline techniques use interferograms with small temporal and spatial baselines to reduce decorrelation. The original small baseline technique [9] uses a network of multilooked small baseline interferograms and the target scatterers are identified by coherence (i.e., complex correlation) criterion [10], [11]. The multilooking is a limiting factor for detecting local deformations. This issue was resolved in [12] with an extended version of small baseline algorithm applied on full-resolution SAR data set. Hooper [13] proposed another new small baseline method in which full-resolution differential interferograms are used to identify stable scatterers incorporating both amplitude and phase criterion. The filtered phase of those pixels that decorrelate little over short time intervals of interferograms, the so-called slowly-decorrelating filtered phase (SDFP) pixels are then used for deformation analysis.

Polarimetric optimization of polarimetric SAR data has been applied to improve classical InSAR results [14], [15] in terms of both deformation estimation and target classification [16], [17]. Optimization can be applied to full polarimetric space-borne SAR data [18], [19], ground-based fully PolSAR acquisitions [20] or compact polarimetric SAR data [21]–[23]. The approach improves the results by finding the scattering mechanism that minimizes decorrelation for each pixel over time, using coherence stability criteria or ADI, thereby maximizing the quality and number of selected PS pixels [17], [22], [24]–[26].

In this letter, for the first time, we have developed a polarimetric optimization approach based on the small baseline
method of the Stanford method for persistent scatterers (PSs) and multitemporal InSAR (StaMPS/MTI) analysis presented in [13]. In our algorithm, instead of applying ADI criterion, we utilize simulated annealing (SA) optimization to minimize the amplitude difference dispersion (ADD) value of each pixel. This can be employed as a rough proxy for phase variance for Gaussian scatterer pixels and it is an indicator for potential of a pixel to be an SDFP candidate, in dual-polarimetry X-band SAR images, followed by projection of the polarimetric interferograms onto the optimized polarimetric channel to reproduce the interferograms with the optimum scattering mechanism. As proposed in [17], SDFP candidates are selected based on lower values of ADD in reproduced interferograms. In an additional step, the phase stability of each candidate is tested using a measure similar to coherence magnitude called temporal coherence [8], [13], defined as

\[ \gamma_x = \frac{1}{N} \sum_{i=1}^{N} \exp \{ j (\phi_{x,i} - \tilde{\phi}_{x,i} - \Delta \tilde{\phi}_{u,x,i}) \} \]  

where \( \phi_{x,i} \) is the wrapped phase of pixel \( x \) in the \( i \)th interferograms, \( \tilde{\phi}_{x,i} \) is the estimate for the spatially correlated terms, \( \Delta \tilde{\phi}_{u,x,i} \) is the estimate of the spatially uncorrelated look angle error term, and \( N \) is the number of interferograms.

For dual-pol SAR data we need to extend the ADD in (1), which is applicable only for single-pol data, also to include dual-pol data and optimize it to increase the density of SDFP pixels for the time-series analysis. We then apply temporal coherence in (2) to identify the SDFP pixels.

Fig. 2 shows a flowchart of the overall processing strategy that is implemented in this letter. The method consists of three main steps: 1) InSAR processing; 2) polarimetric optimization; and (3) multitemporal analysis of the optimized interferograms. Single-pol multitemporal InSAR analysis includes only InSAR processing (step 1) and time-series analysis of the interferograms (step 3). Polarimetric optimization is used here to improve the performance of this analysis using dual-pol data. In Section III we describe in detail the methodology we used in our study.

II. PIXEL SELECTION IN MULTITEMPORAL INSAR

In the StaMPS small baseline method, a set of candidate pixels for time-series analysis are first selected based on the amplitudes of SAR interferograms, to reduce the computational cost time. An index called ADD has been presented (\( D_{AA} \)) to identify SDFP candidates [13]

\[ D_{AA} = \frac{\sigma_{\Delta A}}{\bar{A}} = \sqrt{\frac{\sum_{i=1}^{N}(\Delta A_i - \overline{\Delta A})^2}{\sum_{i=1}^{N}(|M_i| + |S_i|)/2N}} \]  

where \( \sigma_{\Delta A} \) is the standard deviation of the difference in amplitude between master and slave images, \( \bar{A} \) is the mean amplitude, \( \Delta A_i \) is the difference in amplitude between master (\( M_i \)) and slave (\( S_i \)) images, and \( N \) is the number of interferograms.

In this method a higher value of ADD in comparison with ADI, e.g., 0.6 is selected for the threshold and pixels with ADD value less than the threshold are considered as SDFP candidates. The residual phase noise for SDFP candidates is estimated by subtracting two major components of signal: spatially correlated and spatially uncorrelated components. Finally, SDFP pixels are identified among the candidates using temporal coherence [8], [13], defined as

\[ \gamma_x = \frac{1}{N} \sum_{i=1}^{N} \exp \{ j (\phi_{x,i} - \tilde{\phi}_{x,i} - \Delta \tilde{\phi}_{u,x,i}) \} \]  

III. ADD OPTIMIZATION

In order to obtain the polarimetric form of ADD it is sufficient to replace the amplitude of single-pol data in (1) by the polarimetric scattering coefficient, \( \mu \) defined as

\[ \mu = \omega^T K \]  

\[ K = \frac{1}{\sqrt{2}} [S_{hh} + S_{vv}, S_{hh} - S_{vv}]^T \]  

\[ \omega = [\cos(\alpha), \sin(\alpha) e^{i\psi}]^T, \quad 0 \leq \alpha \leq \pi/2, \quad -\pi \leq \psi \leq \pi \]
where $K$ stands for the polarimetric vector, $\omega$ is the polarimetric projection vector, $S_{\text{V}}$ and $S_{\text{hh}}$ are the complex values of the HH and VV channels, respectively, $T$ is the transpose operator and $*$ denotes the conjugate operator. $\alpha$ and $\psi$ are Pauli parameters which represent the scattering mechanism [17], [22], [27]. The polarimetric form of ADD in (1) can then be written in the following form:

$$D_{\Delta A}^\text{Pol} = \sqrt{\frac{\sum_{i=1}^{N} (\Delta A_i^\text{Pol} - \Delta A_i^\text{Pol}')}^2/N}{\sum_{i=1}^{N} (|\omega_T^* K_{\text{V}}^M - |\omega_T^* K_{\text{V}}^N|)}/2N$$

(6)

where $K_{\text{V}}^M$ and $K_{\text{V}}^N$ are polarimetric vectors of master and slave images, respectively.

The main objective of polarimetric optimization is to find the optimum scattering mechanism of the pixels and generate interferograms with better quality than using single-pol SAR images. To simplify the search of the optimum scattering mechanism, we parameterized the projection vector in terms of Pauli basis parameters. In order to build consistent time series of phases related to deformation we assume that the scattering mechanisms of the pixels remain the same during acquisition time, as in the case of multibaseline equal scattering mechanisms. Therefore, $\omega$ would be the same for the pixel in whole stack of interferograms [28].

The optimization problem is to find the projection vector that minimizes the value of ADD. Fig. 3 illustrates the possible ADD values, in terms of $\alpha$ and $\psi$, for three arbitrarily selected pixels in our study area. In [17] we showed that SA is an effective method to minimize such smooth functions as illustrated in Fig. 3 and to find the optimum $\alpha$ and $\psi$ in their corresponding finite range. We define a coarse grid with a step size of 10° for both $\alpha$ and $\psi$ and search for the values that give the minimum ADD. These values for $\alpha$ and $\psi$ are then used as initial values in the SA optimization method.

### IV. Experimental Results and Discussion

To evaluate the method we processed 17 co-polar SAR images acquired by the TerraSAR-X satellite in an ascending mode between July 2013 and January 2014 over the Tehran plain, which is highly affected by subsidence [29]. We formed a small baseline network consisting of 44 single-look interferograms as shown in Fig. 4. We then generated interferograms for HH, VV and optimum channels and calculated the ADD value of each pixel in the single-look interferograms. To evaluate the improvement in ADD, we compared

The histograms of ADD values for HH, VV and optimum channel (Fig. 5).

As shown in Fig. 5, by applying the proposed method, the histogram of ADD values in optimum channel is inclined to lower values of ADD in comparison to HH and VV channels. Therefore, by thresholding ADD value of less than 0.6, more SDFP candidates are extracted in optimum channel as compared to single-pole interferograms.

Fig. 6 depicts the number of selected SDFP candidates obtained from HH, VV and optimum channels using ADD criterion and also the improvement in number of SDFP pixels after utilizing temporal coherency.

The total number of SDFP candidates for the optimum channel is about 2.5 times higher than for the HH and VV channels. Considering the final selection of SDFP pixels for the optimum channel, the number has increased by about 1.4 times and 1.6 times in comparison to the HH and VV channels, respectively.

In order to evaluate the efficiency of using multitemporal polarimetric SAR data for different models of scattering we made a comparison between urban and nonurban regions. 46% of our study area comprises urban region, while the nonurban portion is about 54%. In urban areas, the number of identified candidates using the optimum channel is increased by ~1.7 and ~2.1 times compared to HH and VV channels, respectively. In regard to the agricultural regions, the increase is ~2.1 and ~2.2 times [Fig. 7(b)]. The number of final SDFP pixels increased ~1.4 and ~1.5 times in urban regions and ~1.48 and ~1.65 times in agricultural regions, in comparison

![Fig. 4. Small baselines network used in this letter. The stars denote the SAR images and lines present the formed interferograms for Small Baseline processing.](image)

![Fig. 5. Histograms of ADD for HH, VV and optimum channel.](image)

![Fig. 6. Number of SDFP Candidates and SDFP pixels obtained by HH, VV and optimum channel.](image)
to HH and VV channels, respectively [Fig. 7(a)]. Therefore the proposed algorithm is slightly more successful in nonurban regions than in urban regions.

As PS pixels and SDFP pixels relate to different scattering characteristics of the ground, we also compared the density of measurements for both of the methods in urban and nonurban regions. Table I describes the percentage of additional pixels identified by SDFP pixels in comparison with PS pixels for which the results were previously published in [17]. For the HH and VV channels we detect about 8% more SDFP pixels than PS in agricultural regions, however, over the urban area the number of identified SDFPs is almost 9% less than PS pixels.

Similar to the HH and VV channels, in the case of the optimum channel, the small baseline method detects 10% more coherent pixels in agricultural regions, while in urban area the PS pixels are more numerous than SDFP pixels by about 8%. SDFP pixels show little loss of correlation in short time intervals whereas PS pixels remain stable over the whole period of data acquisition. Therefore, in nonurban area more SDFP pixels are expected to be identified than PS pixels. By contrast, in urban areas PS pixels are more abundant. This might be related to the effect of filtering in the small baseline method, which increases the decorrelation in pixels dominated by a single scatterer as a result of coarsening the resolution of spectra [13].

In order to check that using the optimum channel leads to lower phase noise, we selected SDFP pixels approximately every 0.001° in both directions, and calculated the variance of the phase differences between the selected pixels and their immediate SDFP neighbors for the optimum, HH and VV channels. The results are shown in Fig. 8.

The standard deviation of differences are very similar for HH and VV, but are generally lower for the optimum channel, indicating that our method leads to reduced phase noise. There appear to be two populations of pixels, however; those for which the improvement is marginal and those for which the improvement is more significant [indicated in Fig 8(a)]. This division is not apparently related to scattering mechanism, but does appear to correlate with spatial position (Fig. 9), with pixels in urban areas, plotted in red, more likely to fall in the population with greatest improvement.

Fig. 10 shows the time series for three sample SDFP pixels with odd-bounce (point 1), even-bounce (point 2) and dipole (point 3) scattering mechanisms, respectively.
that were selected using the optimal channel, but not when using HH and VV channels. The smoothness of each of the time series indicates that the phase values have a low contribution from noise and that our algorithm is not increasing the number of selected pixels simply by selecting more noisy pixels.

V. CONCLUSION

StaMPS is a powerful method for multitemporal analysis of single-channel SAR images [13]. In this letter, we have presented a small baseline method, implemented in StaMPS, to deal with dual polarization SAR images. The ADD index criterion is first minimized for dual polarimetric data to find the optimum scattering mechanism that lead to increase the number of SDFP candidates. Then the results are combined with temporal coherence criteria to select final coherent pixels for time-series analysis. Our experiment in both urban and agricultural regions, shows that applying our method for dual-pol data increased the number of SDFP pixels by 50% in comparison to single-pol data InSAR time-series analysis. In addition, the assessment between the result of our proposed method for small baseline algorithm with those from PS-InSAR polarimetric optimization [17], showed that the density of SDFP pixels, in small baseline approach, is more than PS pixels in nonurban regions, while, in urban area the number of PS pixels is slightly higher than the SDFP pixels. Future research could focus on implementing this type of polarimetric optimization on full/quad polarimetry SAR images. Also, joint optimization using the PSI approach [17], [22] and our new algorithm could improve the ability to find stable points for a large range of ground scattering characteristics.

ACKNOWLEDGMENT

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REFERENCES


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where \( \sigma_{\Delta A} \) is the standard deviation of the difference in amplitude between master and slave images, \( \bar{a} \) is the mean amplitude, \( \Delta A_i \) is the difference in amplitude between master \( M_i \) and slave \( S_i \) images, and \( N \) is the number of interferograms. In this method a higher value of ADD in comparison with ADI, e.g., 0.6 is selected for the threshold and pixels with ADD value less than the threshold are considered as SFDP candidates. The residual phase noise for SFDP candidates is estimated by subtracting two major components of signal: spatially correlated and spatially uncorrelated components. Finally, SFDP pixels are identified among the candidates using temporal coherence [8], [13], defined as

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III. ADD OPTIMIZATION

In order to obtain the polarimetric form of ADD it is sufficient to replace the amplitude of single-pol data in (1) by the polarimetric scattering coefficient, \( \mu \) defined as

\[
\mu = \omega^T K
\]

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K = \frac{1}{\sqrt{2}} \left[ S_{hh} + S_{VV}, S_{hh} - S_{VV} \right]^T
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\[
\omega = [\cos(\alpha) \sin(\alpha) e^{j\psi}]^T, \quad 0 \leq \alpha \leq \pi/2, \quad -\pi \leq \psi \leq \pi
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where $K$ stands for the polarimetric vector, $\omega$ is the polarimetric projection vector, $S_C$ and $S_{gh}$ are the complex values of the HH and VV channels, respectively, $T$ is the transpose operator and $*$ denotes the conjugate operator, $\alpha$ and $\psi$ are Pauli parameters which represent the scattering mechanism [17], [22], [27]. The polarimetric form of ADD in (1) can then be written in the following form:

$$D_{\Delta \alpha}^{Pol} = \sqrt{\frac{\sum_{i=1}^{N} (|\Delta A_i^{Pol}| - |\Delta A_i^{Pol}|^2/N}{\sum_{i=1}^{N} (|\omega^T K_i^M| + |\omega^T K_i^S|)/2N}}$$

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**IV. EXPERIMENTAL RESULTS AND DISCUSSION**

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Fig. 7. Number of (a) identified SDFP pixels and (b) SDFP candidates detected in urban and agricultural regions using HH, VV and optimum.

TABLE I

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Agricultural</th>
<th>Urban</th>
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<tbody>
<tr>
<td>HH</td>
<td>8.5 %</td>
<td>-9.0 %</td>
</tr>
<tr>
<td>VV</td>
<td>8.2 %</td>
<td>-8.9 %</td>
</tr>
<tr>
<td>Optimum</td>
<td>10.3 %</td>
<td>-7.9 %</td>
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</table>

to HH and VV channels, respectively [Fig. 7(a)]. Therefore the proposed algorithm is slightly more successful in nonurban regions than in urban regions.

As PS pixels and SDFP pixels relate to different scattering characteristics of the ground, we also compared the density of measurements for both of the methods in urban and nonurban regions. Table I describes the percentage of additional pixels identified by SDFP pixels in comparison with PS pixels for which the results were previously published in [17]. For the HH and VV channels we detect about 8% more SDFP pixels than PS in agricultural regions, however, over the urban area the number of identified SDFPs is almost 9% less than PS pixels.

Similar to the HH and VV channels, in the case of the optimum channel, the small baseline method detects 10% more coherent pixels in agricultural regions, while in urban area the PS pixels are more numerous than SDFP pixels by about 8%. SDFP pixels show little loss of correlation in short time intervals whereas PS pixels remain stable over the whole period of data acquisition. Therefore, in nonurban area more SDFP pixels are expected to be identified than PS pixels. By contrast, in urban areas PS pixels are more abundant. This might be related to the effect of filtering in the small baseline method, which increases the decorrelation in pixels dominated by a single scatterer as a result of coarsening the resolution of spectra [13].

In order to check that using the optimum channel leads to lower phase noise, we selected SDFP pixels approximately every 0.001° in both directions, and calculated the variance of the phase differences between the selected pixels and their immediate SDFP neighbors for the optimum, HH and VV channels. The results are shown in Fig. 8.

The standard deviation of differences are very similar for HH and VV, but are generally lower for the optimum channel, indicating that our method leads to reduced phase noise. There appear to be two populations of pixels, however; those for which the improvement is marginal and those for which the improvement is more significant [indicated in Fig 8(a)]. This division is not apparently related to scattering mechanism, but does appear to correlate with spatial position (Fig. 9), with pixels in urban areas, plotted in red, more likely to fall in the population with greatest improvement.

Fig. 8. Cross comparison of Standard deviation of phase differences of nearby SDFP pixels for the selected SDFP pixels for (a) HH versus optimum channel, the two populations marked by green and red eclipse are spatially located in Fig. 9, (b) VV versus optimum channel, and (c) HH versus VV channel. Blue and red dots indicate odd-bounce and even-bounce scattering mechanisms, respectively. Green and black colors indicate vertical and horizontal dipole scattering mechanism, respectively.

Fig. 9. Spatial position of the pixels in the two populations indicated in Fig. 8(a). Red circles depict the pixels located in the population where the reduction in standard deviation is most significant and the other population members are drawn in green.

Fig. 10 shows the time series for three sample SDFP pixels with odd-bounce (point 1), even-bounce (point 2) and dipole (point 3) scattering mechanisms, respectively.
that were selected using the optimal channel, but not when using HH and VV channels. The smoothness of each of the time series indicates that the phase values have a low contribution from noise and that our algorithm is not increasing the number of selected pixels simply by selecting more noisy pixels.

V. CONCLUSION

StaMPS is a powerful method for multitemporal analysis of single-channel SAR images [13]. In this letter, we have presented a small baseline method, implemented in StaMPS, to deal with dual polarization SAR images. The ADD index criterion is first minimized for dual polarimetric data to find the optimum scattering mechanism that lead to increase the number of SDFP candidates. Then the results are combined with temporal coherence criteria to select final coherent pixels for time-series analysis. Our experiment in both urban and agricultural regions, shows that applying our method for dual-pol data increased the number of SDFP pixels by 50% in comparison to single-pol data InSAR time-series analysis. In addition, the assessment between the result of our proposed method for small baseline algorithm with those from PS-InSAR polarimetric optimization [17], showed that the density of SDFP pixels, in small baseline approach, is more than PS pixels in nonurban regions, while, in urban area the number of PS pixels is slightly higher than the SDFP pixels. Future research could focus on implementing this type of polarimetric optimization on full/quad polarimetry SAR images. Also, joint optimization using the PSI approach [17, [22] and our new algorithm could improve the ability to find stable points for a large range of ground scattering characteristics.

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REFERENCES
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